# Lectures on Economic Inequality

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- Overview: Convergence and Divergence
- Inequality and Divergence: Technical Progress
- Inequality and Divergence: Psychological Factors
- Inequality, Polarization and Conflict
- Uneven Growth and Conflict

# The Fourth Fundamental Law of Capitalism

- In the long-run, technical progress must displace labor.
- Large literature on induced technical change:

Classical: Hicks (1932), Drandakis-Phelps (1965), Kennedy (1964), Salter (1966)

Recent: Autor-Krueger-Katz (1998), Galor-Maov (2000), Acemoglu (1998, 2002)

- Largely taxonomy of technical progress, or reactions to shocks.
- But my comments here on the ultra-long run.

### Outline of the Argument

- Labor is fixed, or grows exogenously.
- Capital is endogenously accumulated.
- In growing economy, the price of capital relative to labor falls.
- Induces technical progress that displaces labor.
- **"Stability argument"**: But too fast, otherwise labor will become too cheap.
- That negates the initial incentive to substitute away from labor.
- So "in equilibrium," displacement happens gradually. But it must happen.

#### More Detail

- For simplicity, fix the labor supply at  $\bar{L}$ .
  - (Can easily have exogenous growth.)
- Output produced by capital and labor using Cobb-Douglas:

$$Y = AK^{\alpha}L^{1-\alpha}$$

• Capitalists accumulate own capital, hire labor at wage w:

$$\max_{L} AK^{\alpha}L^{1-\alpha} - wL$$

■ Indirect linear profit function defined on *K* alone:

$$\pi(\alpha, A, w)K \equiv \alpha A^{1/\alpha} \left(\frac{1-\alpha}{w}\right)^{(1-\alpha)/\alpha} K.$$

• w is going to be endogenously pinned by  $\bar{L}$  (later).

■ Capitalists choose an accumulation path  $\{K_t\}$  to maximize

$$\sum_{t=0}^{\infty} \delta^{t}(\text{Dividends})_{t} = \sum_{t=0}^{\infty} \delta^{t} \left[ \pi(\alpha, A, w_{t}) K_{t} - K_{t+1} - c(I_{t}) \right],$$

- where  $K_{t+1} = (1-d)K_t + I_t$  and  $I_t \ge 0$ ,
- $\{w_t\}$  is fully anticipated, and
- c is strictly convex with c(0) = c'(0) = 0 and  $c'(\infty) = \infty$ .
- **Equilibrium condition:**  $L_t = \bar{L}$  for all t.

In long run steady state,  $K_t \to K^*$  such that

$$\delta\pi(\alpha, A, w^*) = \delta\alpha A^{1/\alpha} \left(\frac{1-\alpha}{w^*}\right)^{(1-\alpha)/\alpha} = 1.$$

which is the modified golden rule, and

$$(1-\alpha)A(K^*/\bar{L})^{\alpha}=w^*,$$

- which is static profit maximization.
- Now introduce some exogenous growth just as in Solow:
- $A_t < A_{t+1} \text{ for all } t, \text{ and } A_t \to \infty.$
- Then "in the long run"  $w_t$  chases  $A_t$  to maintain the equality

$$\delta \alpha A_t^{1/\alpha} \left( \frac{1-\alpha}{w_t} \right)^{(1-\alpha)/\alpha} = 1,$$

■ and in particular,  $w_t \rightarrow \infty$ .

■ The "chasing relationship":

$$\delta \alpha A^{1/\alpha} \left( \frac{1-\alpha}{w(A)} \right)^{(1-\alpha)/\alpha} = 1,$$

- **Proposition.** For each  $\alpha$ , there is a threshold  $A^*(\alpha)$  such that
- $\pi(\alpha, A, w(A))$  is decreasing in  $\alpha$  when  $A < A^*(\alpha)$ , and
- $\pi(\alpha, A, w(A))$  is increasing in  $\alpha$  when  $A > A^*(\alpha)$ .
- Intuition. w(A) rises faster than A, benefiting from both technical progress and capital accumulation.

- Implication of Proposition.
- If  $\alpha$  endogenously chosen at some cost, the share of capital income in total income will go to 1. [Limit Robotic Economy.]
- (But not too fast ... w still has to climb on transition path.)
- Unbounded functional inequality, can translate into unbounded personal inequality if combined with earlier arguments.