

Lectures on Economic Inequality

Warwick, Summer 2016, Supplement to Slides 3

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- Overview: Convergence and Divergence
 - Inequality and Divergence: Economic Factors
 - [Inequality and Divergence: Psychological Factors, Part 2](#)
 - Inequality, Polarization and Conflict
 - Uneven Growth and Conflict
-
- Recall alternative approaches to the study of poverty
 - [Constraints](#)
 - absence of credit
 - absence of insurance
 - nonconvexities (nutrition, health, education)
 - [Psychology](#)
 - failed [aspirations](#)
 - [informational](#) biases
 - temptation, lack of [self-control](#)

Two Examples from Developing Countries

- Poor forego **profitable small investments**
 - Agricultural investment in Ghana (Udry-Anagol, 2006)
 - Fertilizer use in Kenya (Duflo-Kremer-Robinson, 2010)
 - Microenterprises in Sri Lanka (Mel-McKenzie-Woodruff, 2008)
- **Public distribution** debate
 - Public food distribution system in India
 - Huge debate on food versus cash transfers
 - Impulsive spending from cash (Khera 2011 survey)

Self-Control or Just Present Bias?

- Demand for **commitment products** in LDCs.
 - Lockboxes in the Gambia (Shipton, 1992)
 - Commitment savings in the Philippines (Ashraf-Karlan-Yin, 2006)
 - ROSCAS (Aliber, 2001, Gugerty, 2001, 2007, Anderson-Baland, 2002)
- **Pressures to share**
 - Extended-family demands on wealth
 - (Platteau 2000, Hoff-Sen 2006, Brune et al 2011)

Preferences: The “Shape” of Temptation

Based on Banerjee-Mullainathan (2010) [BM]

- “The link to poverty within this framework comes from **assuming** that the fraction of the marginal dollar that is spent on temptation goods can depend on the level of consumption.”

- Divide assets A into consumption c and bequest b :

$$A = c + b$$

while new assets A' are a random variable given by

$$A' = f(b, \theta).$$

- View as wealth plus labor income, so $f(0, \theta)$ generally positive.

- BM write

$$c = x + z$$

where x is a standard good and z is a **temptation good**.

- Two-period model. In period 2, agent maximizes

$$U(x_2) + V(z_2), \text{ subject to } x_2 + z_2 = A'.$$

- Let $x(A')$ and $z(A')$ be resulting consumption functions.

- In period 1, agent does not value $V(z_2)$, so maximizes

$$U(x_1) + V(z_1) + \delta EU(x(A')) = U(x_1) + V(z_1) + \delta EU(x(f(b, \theta))),$$

subject to the constraint $x_1 + z_1 + b = A$.

- Leads to the first-order condition:

$$\begin{aligned} U'(x_1) = V'(z_1) &= \delta EU'(x(f(b, \theta)))f'(b, \theta)x'(f(b, \theta)) \\ &= \delta EU'(x(f(b, \theta)))f'(b, \theta)[1 - z'(f(b, \theta))], \end{aligned}$$

which BM call the **modified Euler equation**.

- Obviously, similar equation would hold in multi-period model.

Some Immediate Implications

- The **desire to commit**.
 - Doesn't fully emerge in this framework because commitment blocks both x - and z -consumption.
 - But would commit if it could protect x -consumption and hinder z -consumption.
 - Example: purchase of **durable goods** today.
- The effect of **sin taxes**.
 - Imagine a future tax on period-2 consumption of z .
 - Effect on savings will depend on what happens to derivative $x'(A')$.
 - Could go up or down.

The Shape Assumption

- Note that the formulation does not restrict curvature of $x(A')$ or $z(A')$ in any way.
- **Main assumption.** z is strictly concave.
 - Temptation matters less at the margin as assets go up.
 - BM justify this by saying that:
 - temptations are visceral and kick in more at low incomes.
 - temptation goods are more divisible
 - "it may be easier for a rich person to say no to a relative who wants a few hundred dollars ... than for a poor person to refuse one who wants just a couple of dollars for a meal."
- Without commenting on any of this, let's just say it's an empirical question.

Implications of the Shape Assumption

- (Under additional presumption that Euler equation still valid.)

- The poor appear **more impatient**.

- Proof: effective discount factor given by

$$\hat{\delta} = \delta x'(A').$$

- Possible **anti-smoothing** of consumption.

- Raise future labor income by uniformly raising $f(0, \theta)$.

- In standard model with no z , consumption today \uparrow (smoothing).

- Here this might flip: countervailing effect given by the fact that $z'(A')$ flattens.

- So modified Euler equation could generate more saving.

- **Poverty traps.**

- Reconsider maximization problem:

$$U(x_1) + V(z_1) + \delta EU(x(f(b, \theta))),$$

subject to the constraint $x_1 + z_1 + b = A$.

- Write $c_1 = x_1 + z_1$ let W be indirect utility function, so maximize

$$W(c_1) + \delta EU(x(f(b, \theta))),$$

subject to $c_1 + b = A$.

- Recall monotonicity lemma: $b(A)$ nondecreasing in A .

- If x is concave, then the problem is concave and no jump in b .

- But if z is concave, b could jump up.

- Interpreted as a “poverty trap.”

■ Possible Lack of **Prudence**.

- An increase in income uncertainty encourages savings in a safe technology:
- Needs a third-derivative restriction on the utility function.
- No longer sufficient in this case.

■ Investment **Scale**.

- Suppose an investment is feasible, has a given return and upper bound on scale.
- In standard model, the upper bound is unimportant in decision to invest.
- Here an increase in the bound can matter, as it lowers the “temptation derivative” $z'(A')$.

■ Adverse effects of **credit**.

- Today’s self can become worse off if tomorrow’s self has access to credit.
- Need a three-period model (at least) for this.
- BM show that with declining temptations, period-0 self might allow period-1 self to have a big loan (and so get temptation to decline) rather than a small loan which will all be blown on the z -good.

- All the results depend on assuming that **the poor are more tempted than the rich**.
- This begs the main question.
- Bernheim, Ray and Yeltekin (1999, 2013) take a different approach.
- They assume that the underlying model is homothetic in preferences.
- The only non-homothetic feature is an imperfect credit market.

Assets and Incomes

- Accumulation

$$A_t = c_t + \frac{A_{t+1}}{\alpha}.$$

- Imperfect credit market

$$A_t \geq B > 0.$$

- **Interpretation:** A = financial assets + pv of labor income

$$P = \frac{\alpha}{\alpha - 1} y,$$

- and

$$B = \Psi(P)$$

- e.g.,

$$B = \psi P \text{ for some } \psi \in (0, 1]$$

Preferences $u(c) = c^{1-\sigma}/(1-\sigma)$, for $\sigma > 0$.

$$u(c_0) + \beta \sum_{t=1}^{\infty} \delta^t u(c_t), \quad 0 < \beta < 1.$$

- Standard model: $\beta = 1$.
- If $\delta\alpha > 1$ [**growth**] and $\mu \equiv \frac{1}{\alpha}(\delta\alpha)^{1/\sigma} < 1$ [**discounting**], then

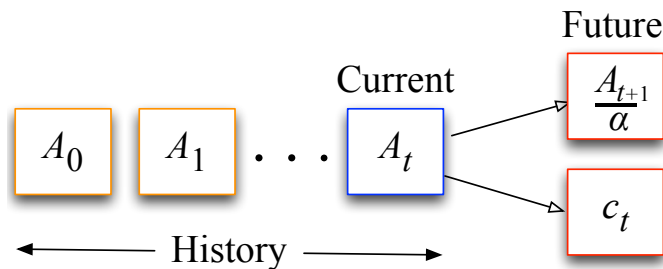
$$A_{t+1} = (\delta\alpha)^{1/\sigma} A_t$$

$$c_t = (1 - \mu)A_t.$$

- \rightarrow **Ramsey policy**.
- If $\beta < 1$, optimal plan is **time-inconsistent**.

Policies and Values

- **Policy** ϕ specifies continuation asset A_{t+1} after every history



- And so generates **values** and **payoffs**:

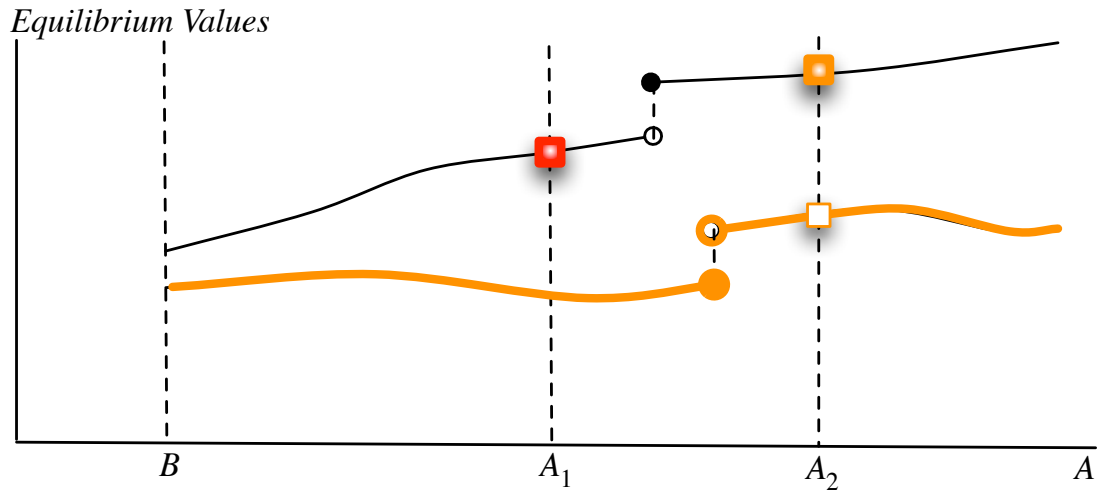
$$V(h_t) \equiv u(c_t) + \delta u(c_{t+1}) + \delta^2 u(c_{t+2}) + \dots$$

$$P(h_t) \equiv u(c_t) + \beta [\delta u(c_{t+1}) + \delta^2 u(c_{t+2}) + \dots] = u(c_t) + \beta \delta V(h_t, \phi(h_t))$$

- **No self-starvation**: $c \geq \nu A$ for some ν tiny but positive.

Equilibrium

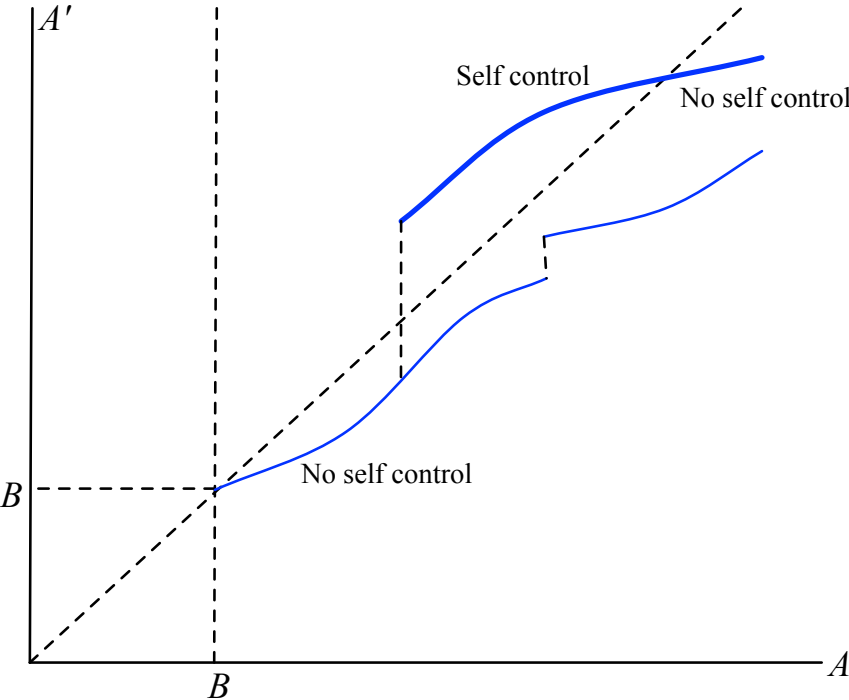
- Following the policy is better than trying something else.
- $P(h_t) \geq u\left(A(h_t) - \frac{x}{\alpha}\right) + \beta\delta V(h_t, x)$ for every $x \in [B, \alpha A(h_t)]$.



Self-Control Definition

- Self-control at A :
 \Rightarrow Accumulation at A in **some** equilibrium.
 - Strong self-control at A :
 $\Rightarrow A_t \rightarrow \infty$ from A , in **some** equilibrium.
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- No self-control at A :
 \Rightarrow No accumulation at A in **any** equilibrium.
 - Poverty trap at A :
 \Rightarrow Slide to credit limit B from A in **every** equilibrium.

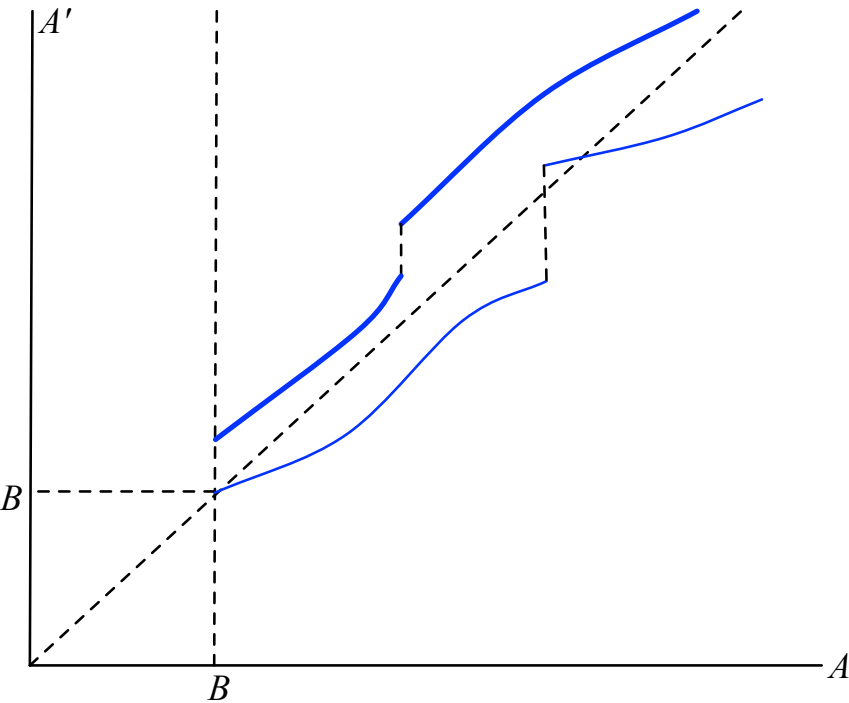
Self-Control and No Self-Control



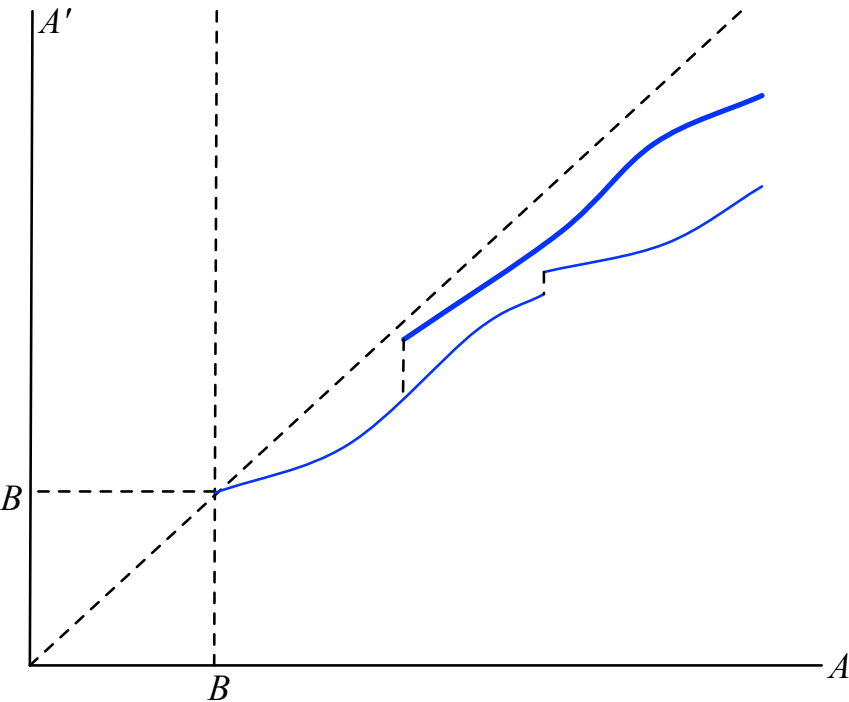
Uniformity and Nonuniformity

- **Uniform** case:
 - Self control at every A , or its absence at every A .
- **Nonuniform** case:
 - Self-control at A , no self-control at A' .

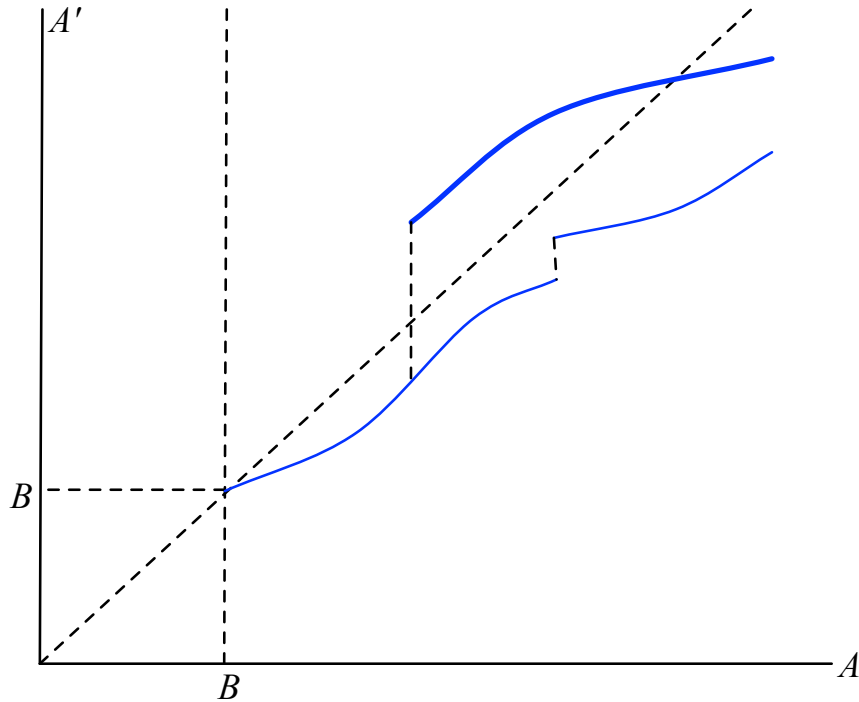
Uniformity and Nonuniformity



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Uniformity and Nonuniformity



Uniformity and Nonuniformity

■ Uniform case:

- Self control at every A , or its absence at every A .

■ Nonuniform case:

- Self-control at A , no self-control at A' .

■ **Theorem.** Suppose no credit constraints, so that $B = 0$.

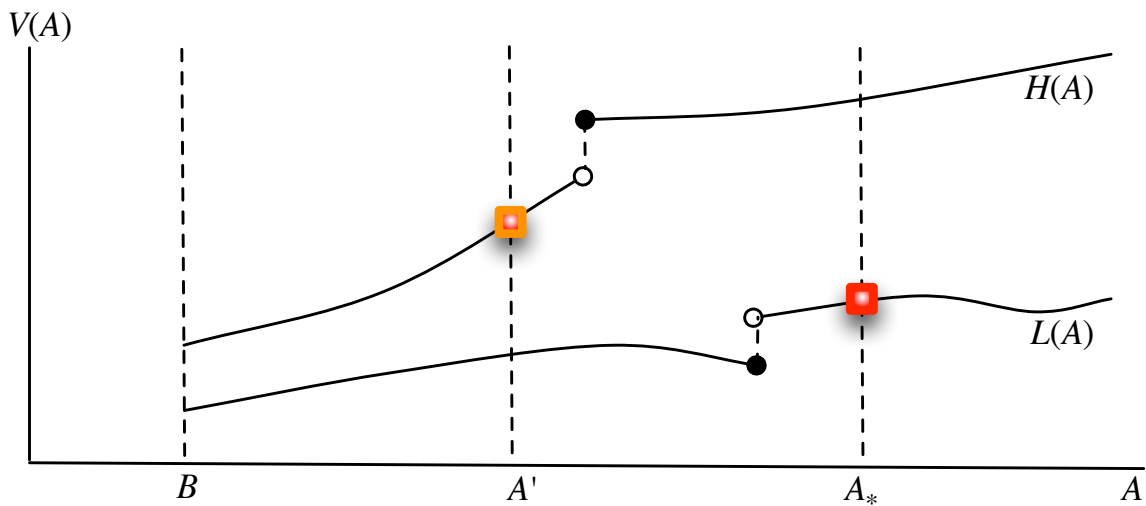
- Then every case is uniform.

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- Poverty bias not built in; contrast Banerjee and Mullainathan (2010).

Credit Constraints and Non-Uniformity

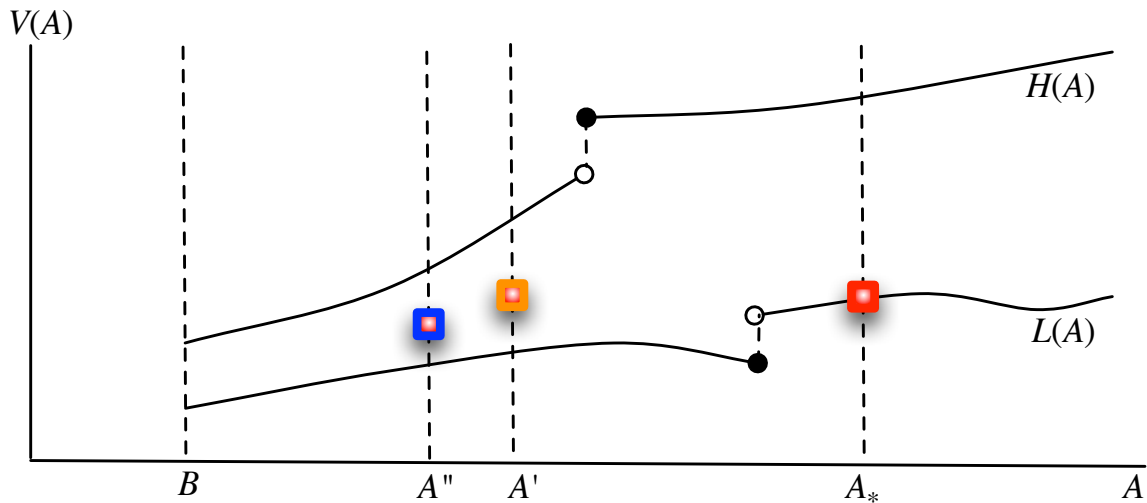
- $B > 0$ destroys scale-neutrality (in A), but how exactly?
- **Some intuition:**
 - Think of the consequences of a **lapse** in self-control.
 - More severe when the individual has more assets; hence more to lose.
- **Problem:**
 - Not bad as intuition, but unfortunately does not work.
 - Severity isn't monotone in assets.
 - To see this, first we understand the structure of worst punishments.

The Structure of Lowest Values



- **Theorem.** If $A' > B$ is continuation for A_* under lowest value at A_* , then A' is followed by value $H^-(A')$.

The Structure of Lowest Values



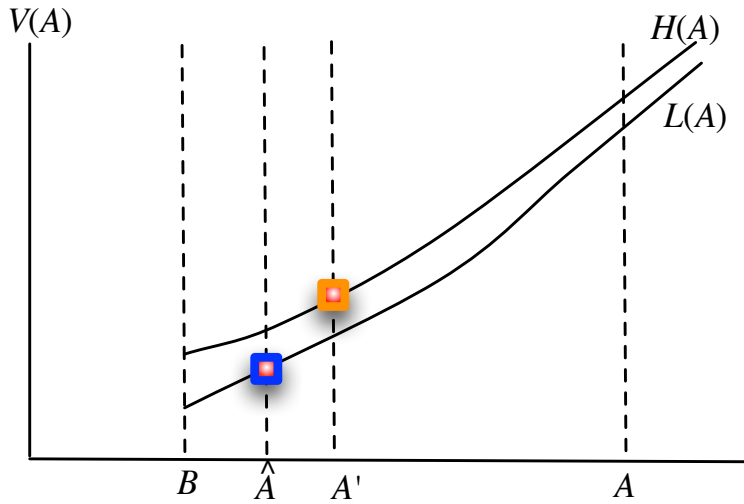
■ **Theorem.** If $A' > B$ is continuation for A_* under lowest value at A_* , then A' is followed by value $H^-(A')$.

$$u(c'_t) + \beta\delta\text{Blue} = u(c'_t) + \beta\delta\text{Orange} \Rightarrow u(c''_t) + \delta\text{Blue} < u(c'_t) + \delta\text{Orange}.$$

Lowest Values

- Simple structure. Following a deviation:
- One more binge, then the highest-value program.
- Like Abreu penal codes, but for entirely different reasons.
- Argument also reveals why $L(A)$ jumps up occasionally.

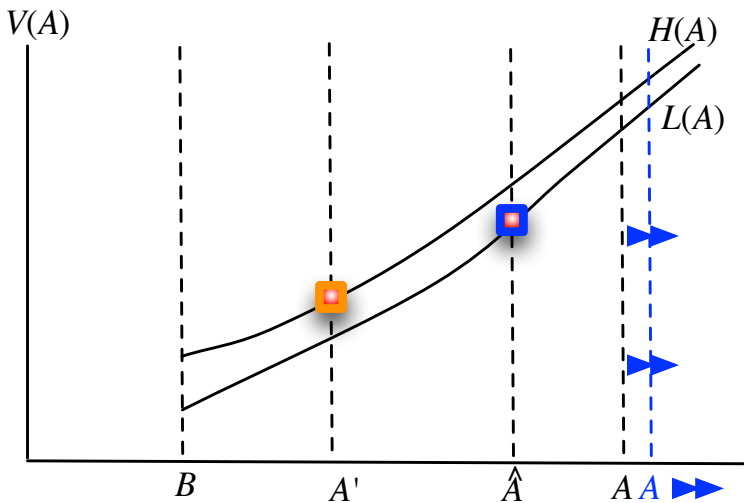
- maximize $u(A - x/\alpha) + \beta\delta L(x)$, say max at $x = \hat{A}$.



- Not possible; get a contradiction:

$$u(\hat{c}_t) + \beta\delta\text{Blue} \leq u(c'_t) + \beta\delta\text{Orange} \Rightarrow u(\hat{c}_t) + \delta\text{Blue} < u(c'_t) + \delta\text{Orange}.$$

- maximize $u(A - x/\alpha) + \beta\delta L(x)$, say max at $x = \hat{A}$.

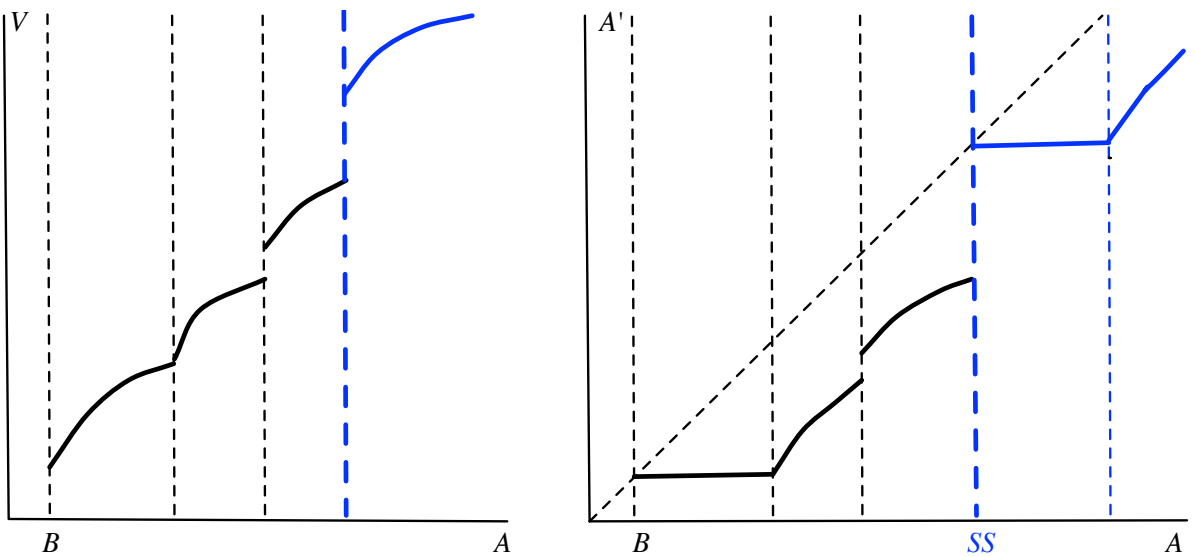


- So $\hat{A} > A'$, and $u(\hat{c}_t) + \beta\delta\text{Blue} = u(c'_t) + \beta\delta\text{Orange}$.
- By concavity of u , A' may need to jump up, so $L(A)$ jumps too.

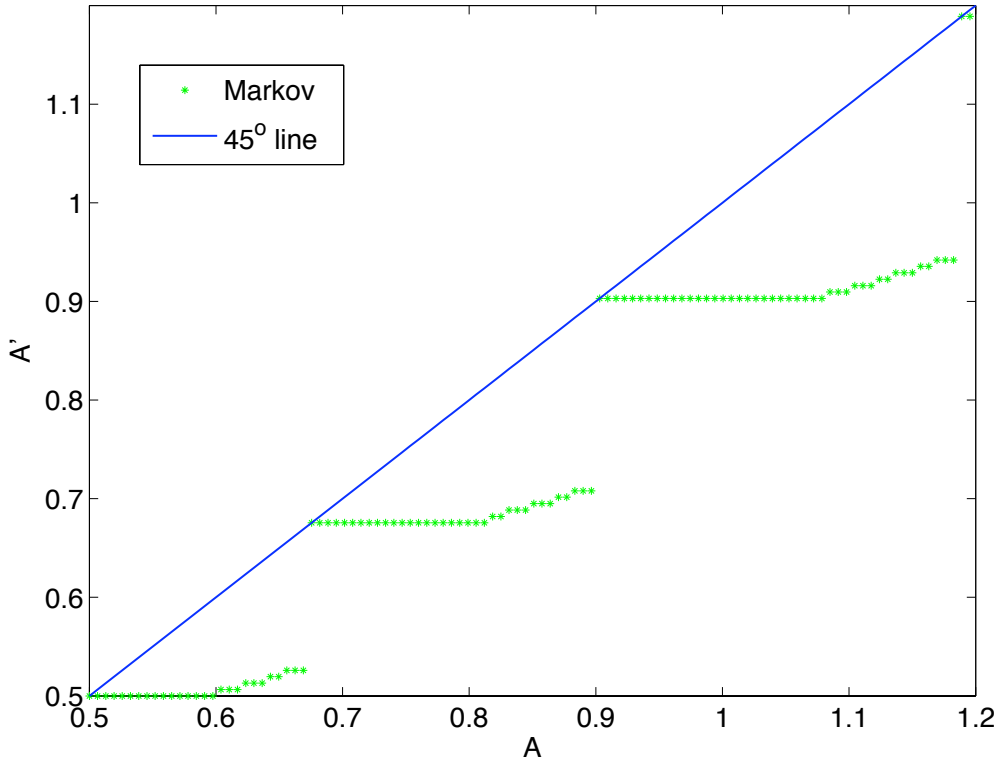
Argument So Far

- The problem of internal self-control is both **simple** and **complex**.
- **Simple**: what happens after lapse of control is easy to describe.
- Lapse followed by **one** round of high c , then back to best path.
- **Complex**: jump in worst values makes comparative statics hard.
- As wealth goes up, can get cycles of control / failure of control.

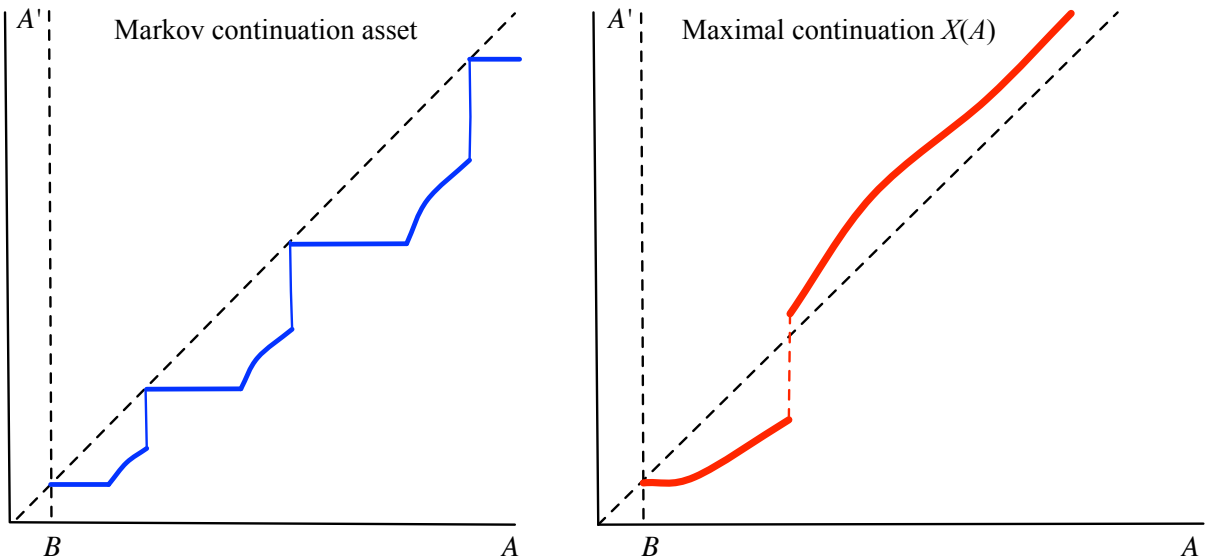
Markov Equilibrium: Values and Continuations



Markov Perfect Equilibria: Savings Function, $\beta=0.75$, $\alpha=1.28$, $\delta=0.8$

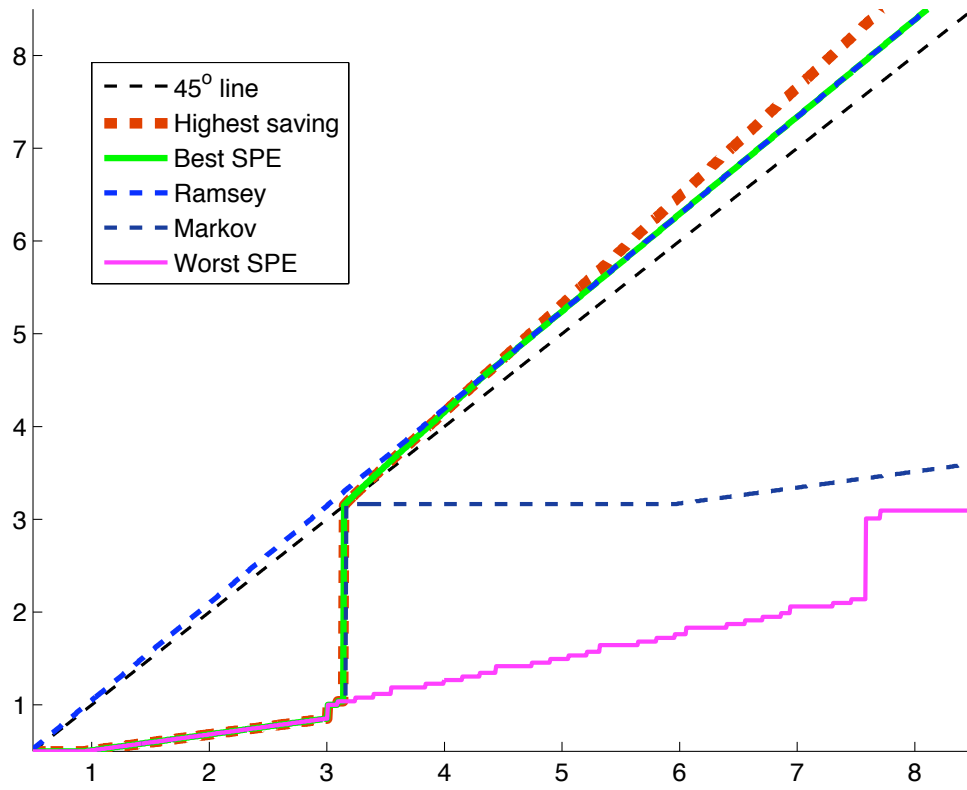


■ Illustration of the nonuniform case:

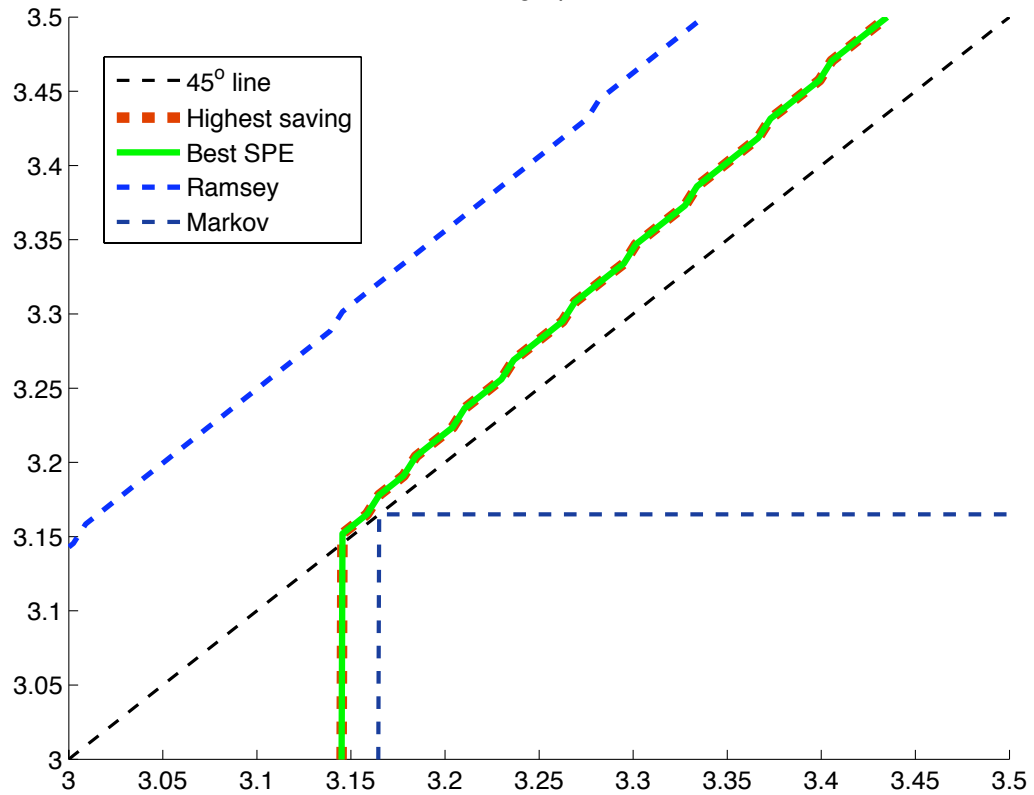


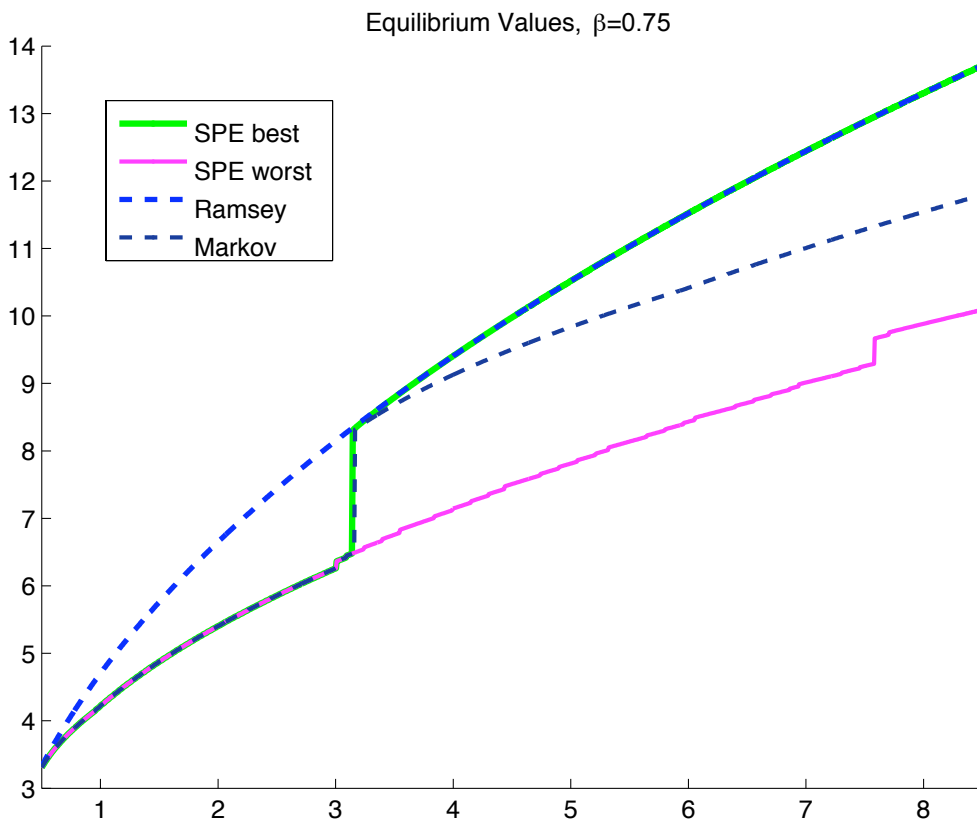
■ But the simulations suggest that this is **not true** with history-dependent strategies.

Savings, $\beta=0.75$



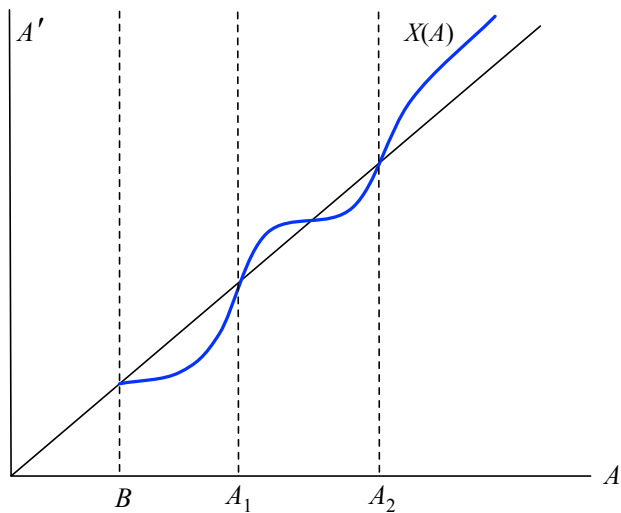
Savings, $\beta=0.75$





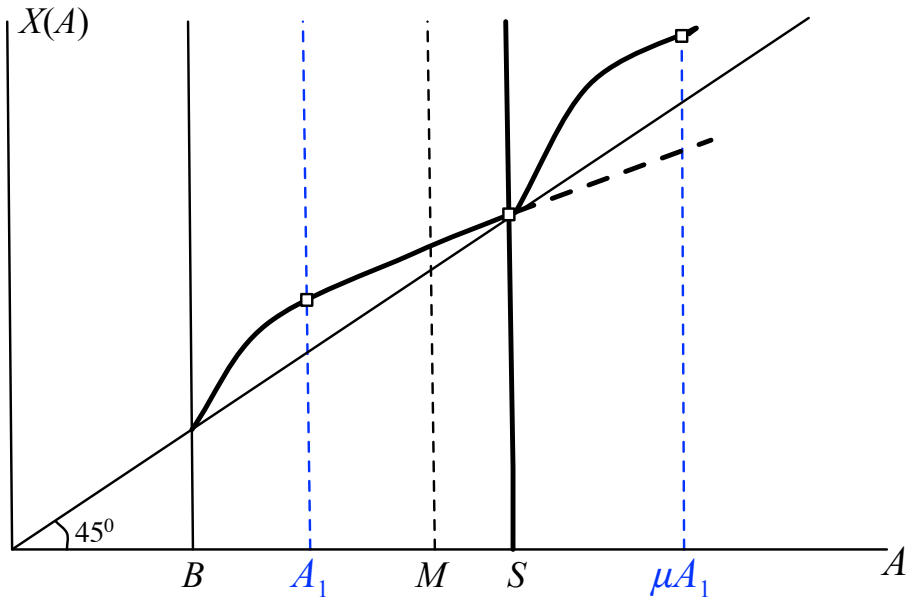
■ **Theorem.** [Central Result]. In the non-uniform case,

- There is $A_1 > B$ such that every $A \in [B, A_1)$ exhibits a **poverty trap**.
- There is $A_2 \geq A_1$ such that every $A \geq A_2$ exhibits **strong self-control**.

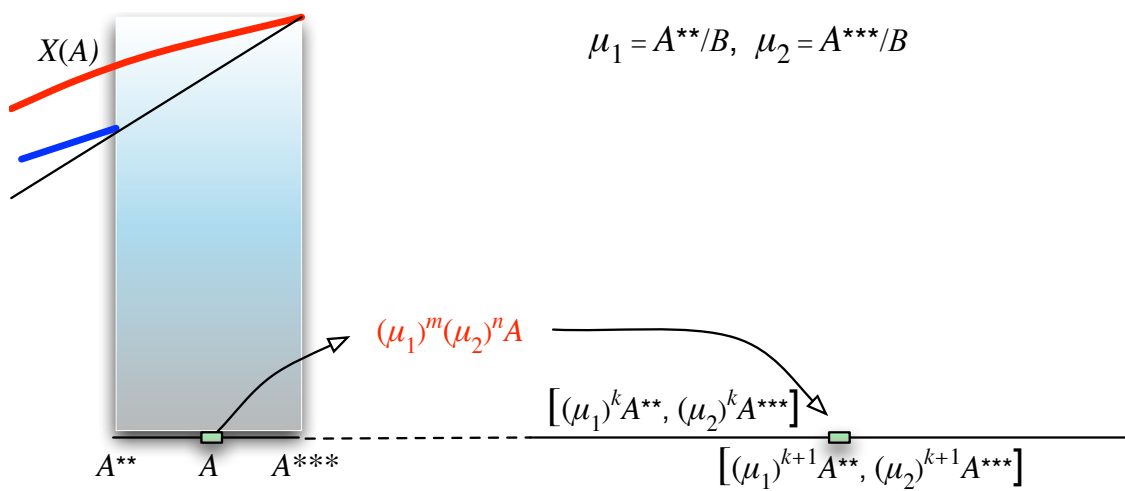


■ **Proof Outline I. The Poverty Trap**

- $X(A)$: maximum wealth choice. Then $X(A) < A$ close to B .



■ **Proof Outline II. Strong Self-Control, contd.**



Some Implications

1. Easier Access to Credit Has Ambiguous Effects

- Conventional theory: more abundant credit reduces saving.
- Implications here are more nuanced.
- Modified neutrality: only B/A matters.
- Easier credit (lower B) reduces A_1 and A_2 thresholds:
- More individuals successfully exercise self-control
- Offsetting effect: those who fall into trap will fall further.
- **Summary**: ambiguous effects, depending on where you start.

2. The Demand for Commitment Devices

- Demand for external commitment devices by poor households.
- Surprisingly little evidence that this demand is more widespread.
- (But: Ariely-Wertenbroch 2002, Beshears-Choi-Laibson-Madrian 2011)
- Need **some** reliance on internal mechanisms (value of flexibility).
- But external devices undermine efficacy of internal mechanisms.
- Who demands external devices?
- The **asset-poor**, and the **income-rich** if $B \propto$ permanent income.
- The **asset-rich** or the **income-poor** prefer internal mechanisms.
- Income-rich generally also asset-rich, so net effect is ambiguous.

3. Designing Accounts to Promote Saving

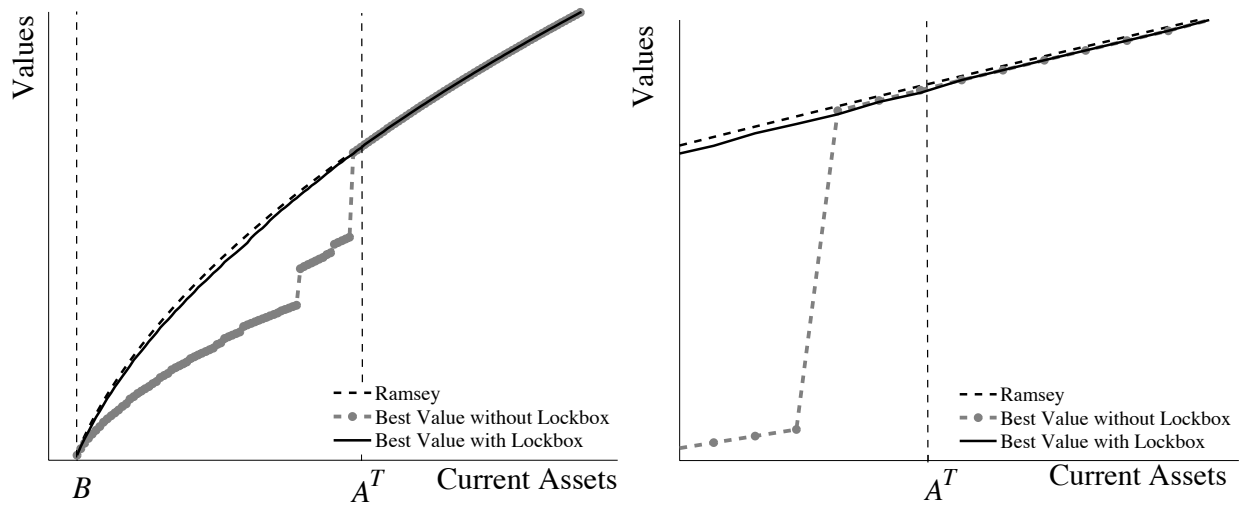
- **Example:** retirement savings programs.
 - Significant variation in lock-up across plans
 - In addition, large variation in stringency of contributions.
- Recall: lock-up has both upside and downside.
 - Programs that capitalize on upside while avoiding downside?
 - **Idea:** lock up funds until some target, then remove the lock.
 - Can (should) allow each individual to select personal target.

- To formalize, use taste shock for uncertain environment:

$$u(c, \eta) = \eta \frac{c^{1-\sigma}}{1-\sigma},$$

- Lock-up account that unlocks once a threshold is reached.
- Threshold slightly higher than the threshold that permits accumulation.
- If lower, the agent will slide back once the account is unlocked.
- Note: nowhere close to solving the optimal design problem.

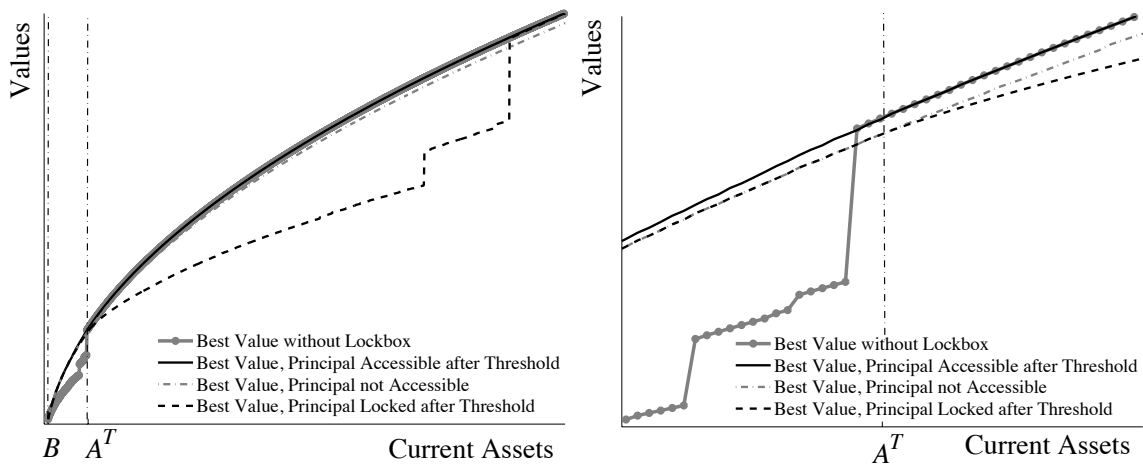
Alternative A. commitment savings up to threshold, full release thereafter.



■ Both the lock-up and the release are important ...

Alternative B: commitment savings forever, principal always locked.

Alternative C: usual saving after threshold, commitment principal locked.



Note: Alternative C can be worse than Alternative B.

4. Asset-Specific MPCs

- Hatsopoulos-Krugman-Poterba (1989), Thaler (1990), Laibson (1997)
- $A = \text{financial assets} + \text{permanent income}$.
- Jump in financial assets
- $B/A = B/(\text{financial assets} + \text{permanent income})$.
- B/A falls: can switch from decumulation to accumulation.
- So low MPC from financial assets.
- Jump in income. If $B/(\text{perm inc})$ constant, $B/A \uparrow$.
- High MPC in non-uniform case.
- At best B unchanged; then identical MPCs.

Summary

- We know that a failure of self-control can lead to poverty.
- Is the opposite implication true?
- Model constructed for scale-neutrality:
- Result isn't "built-in" by presuming that the poor are tempted more.
- Ainslee's personal rules as history-dependent equilibria
- Structure of optimal personal rules is remarkably simple:
- Deviations entail "falling off" the wagon, then "climbing back on".

- **Main result:** ability to impose self-control rises with wealth.
- In fact, the model generates a poverty/self-control **trap**.
- Novel policy implications:
 - Among them: interplay between **external and internal commitments**
 - External self-control devices can undermine internal self-control
 - Lock-box savings accounts with self-established targets and **unlocking of principal** may be particularly effective devices for increasing saving